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ENERGY BENCHMARKING IN A PORTFOLIO OF EDUCATIONAL BUILDINGS IN BRAZIL USING SUPPORT VECTOR MACHINE AND DATA ENVELOPMENT ANALYSIS

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ABSTRACT

Buildings are one of the largest energy consumers in developed countries as well as in Brazil, and no other segment has such a potential for improving energy efficiency. Several policies have been applied for this purpose around the world and energy benchmarking is one of the most used worldwide. Thus, this paper brings a new benchmarking approach that involves not only energy consumption, but it also evaluates managerial issues in energy. For this, Support Vector Machine was used in order to predict the energy consumption using data of vocational schools in the São Paulo state, Brazil, to validate the methodology and Data Envelopment Analysis was used for the elaboration of the efficiency scale. It were considered 92 school buildings for the development of the predictive model and 72 for elaborating the efficiency scale in DEA. The results indicated a great potential for saving energy and financial resources when compared to the best practices.

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INTRODUCTION

Buildings represent one of the largest sectors in terms of energy consumption. In general, in developed countries the share of energy consumption of the building sector is between 20% and 40% of the final energy consumption (Pérez-Lombard *et al.*, 2008). In Brazil, buildings are also among the largest energy consumers and the sector accounted for 51% of the total electricity consumption in 2016 (EPE, 2017). Energy efficiency in existing buildings represents one of the most important research areas in the energy field (WANG and XIA, 2015), and no other area has such a great potential for improvements (ÜRGE-VORSATZ *et al.*, 2009). However, only an evaluation of the projects can be insufficient due to the difference between the expected consumption in the project and in the occupation phase, a phenomenon known as performance gap, described by Olivia and Christopher (2015) and Brady and Abdellatif (2017). Several policies are used to establish efficient buildings, such as benchmarking, which is defined by Spendolini (1992) as a process of comparing products and services against the best practices, and are

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discussed by Pérez-Lombard *et al.* (2009), Chung (2011) and Borgstein *et al.* (2016). Much effort has been made in order to understand the complexity of energy consumption in buildings and also to search for mechanisms to predict energy consumption (Wei *et al.*, 2018). Machine learning (ML) algorithms have been widely used for this purpose (GALLAGHER *et al.*, 2018), they use data from the past aiming to "learn" a pattern of energy consumption and then predict future values of it (AMASYALI and EL-GOHARY, 2018). Comparative analysis between ML algorithms for energy consumption prediction in buildings were performed by Molina-Solana *et al.*, (2017), Robinson *et al.* (2017), Wang and Srinivasan (2017) and also Wei *et al.* (2018). The Support Vector Machine (SVM) algorithm, proposed by Cortes and Vapnik (1995), has risen great interest given its great performance in the most diverse fields (ČEPERIC *et al.*, 2017), and has been used to predict energy consumption in buildings by Jung *et al.* (2015), Paudel *et al.* (2017) and Zhang *et al.* (2016). Another important approach, Data Envelopment Analysis (DEA) proposed by Charnes *et al.* (1978), based on Farrell (1957), refers to an efficiency oriented approach in a set of entities called Decision Making Units (DMU), which relates inputs to output products (COOPER *et al.*, 2011). Although it can be seen as a production frontier evaluation tool, it can be considered that its goal is to evaluate the

organizational performance against the best practices (COOK *et al.*, 2014). DEA is a tool based on optimization in mathematical programming that, according to Chung (2011), has as its main advantage the non-parametric treatment, which does not assume any particular functional form. Although there are variants, the two classic models are the Constant Return to Scale (CRS) model and the Variable Return to Scale (VRS) model proposed by Banker *et al.* (1984), which substitutes the axiom of proportionality between inputs and outputs from the axiom of convexity, in both cases two approaches concerning to orientation are possible, the so-called input orientation, that seeks to minimize input values for the same production of output, and the output orientation, where the inverse analysis is observed. A problem of this methodology is its benevolent character that results in a large number of efficient DMUs, which makes the analysis more difficult, especially when it is intended to order the DMUs by efficiency. That can be overcome by some methods discussed by Angulo-meza *et al.* (2002). One used method is known as super-efficiency (SE-DEA), proposed by Andersen and Petersen (1993), and its basic idea is that the evaluated DMU is excluded from the reference set, allowing even higher values than the maximum value without changing the ordering of the others. In this sense, this paper brings a new methodology for the evaluation of energy performance and benchmarking in a portfolio of buildings, taking as case of study buildings that dwells vocational schools in the São Paulo, Brazil, using SVM to predict energy consumption, and DEA for the efficiency analysis and benchmarking by characteristic features.

MATERIALS AND METHODS

In general, the methodology was based on four pillars: preparation stage, development of the predictive model, the construction of the features to characterize the performance in the management and energy consumption, and finally the benchmarking and the construction of the efficiency scale. An overview of the methodology is shown in Figure 1.

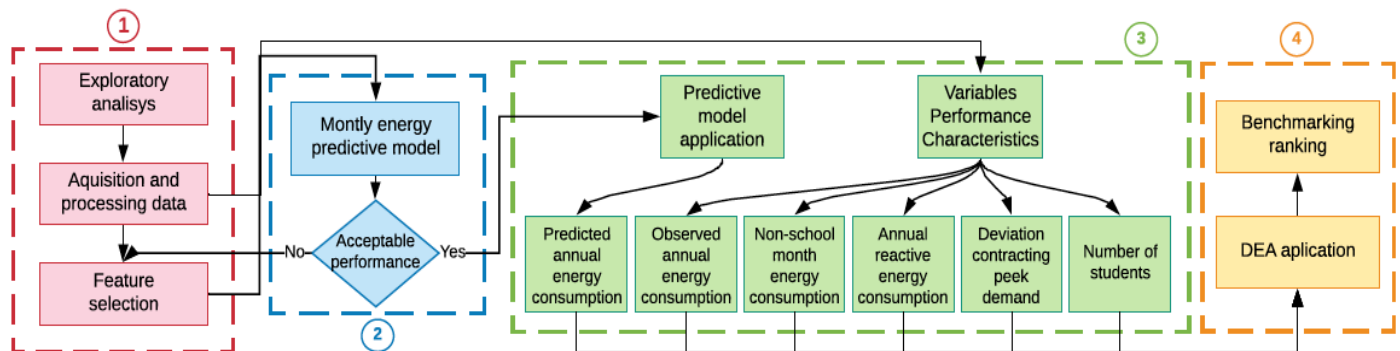


Figure 1. Block diagram of the proposed methodology

Preparation: An exploratory analysis on the typology of the buildings of the portfolio is done aiming the understanding of the energy flows, profiles of use and occupancy, and the hypothesis formulation about the features that can affect the performance. Features related to the constructive attributes, infrastructure, use profile, energy and climatic characteristics were collected for testing and construction of the predictive model. The initial data treatment consisted of removing the missing and the outliers. The interquartile range, also applied by Liu *et al.* (2017), was used in order to identify outliers. Since an excessive number of predictor features may worsen the performance of the model, due to overfitting (Liu *et al.*,

2017), the Pearson Correlation coefficient (r) was used as a selection criterion, as done by Capozzoli *et al.* (2015) and Deng *et al.* (2018), and then the features whose r value were larger than 0.20 were included in the model. The correlation between the input features, a problem known as multicollinearity, should also be avoided in order to keep the quality of the model. The creation of auxiliary features and combination of features can also act positively. Then, climatic, and usage and occupancy features were created for statistical tests.

Development of the predictive model: The predictive model was built using the SVM to predict the monthly energy consumption for each building given their characteristics. Some metrics are usually used to evaluate predictive models and are discussed by Amasyali and El-Gohary (2018). For the evaluation of the proposed model, the Coefficient of Determination (R^2), the Root Mean Square Error (RMSE) and the Coefficient of Variation of RMSE (CV-RMSE) were used.

Features of energy performance: Features were developed in order to characterize the performance in the management and energy consumption of the buildings, which were used in the DEA benchmarking. They are described below as follows:

Annual actual energy (AAE_obs): the sum of the actual monthly energy consumption for a period of twelve months.

Annual predicted energy (AAE_pred): the sum of the monthly active energy consumption predicted by the predictive model for each vocational school building, developed over a period of twelve months.

Annual reactive surplus energy (RAE): the sum of the monthly energy consumption of reactive surplus that exceed the Power Factor limit of 0.92, based on energy bills for a period of twelve months.

Peak demand deviation (PDD): the difference between the ideal value calculated (PDS) for a period of twelve months and the contracted peak demand (PDC). In the Brazilian electricity tariff model, customers of group A must contract the maximum demand power and the whole amount is charged, being either used or not, incurring in a fine if the tolerance of 5% is exceeded. This fine is equivalent to twice the unit value of the contracted demand. The determination of the ideal demand assesses whether the measured demand is less or greater the contracted demand and complements the value to the corresponding feature, if the measured demand is greater

than the contracted demand the difference is considered twice. Thus, the value of PDD is defined as Equation 1.

$$\text{If } PDC \geq PDS: PDD = PDC - PDS \quad (1)$$

$$\text{If } PDC < PDS: PDD = 2 \times (PDS - PDC)$$

Average active energy during non-school months (AEN_{nsm}): the average energy consumption during the non-school months (January, July and December).

Total number of students (TNS): total number of students of each vocational school building.

Energy benchmarking using DEA: The energy benchmarking was based on DEA, taking each vocational school building as a DMU and using the constructed features in order to characterize the energy performance. The model for analysis of efficiency should consider the inputs and outputs in order to obtain the efficiency of each DMU to elaborate the efficiency scale. Thus, input features should tend to minimum values while output features should tend to maximum values. The model was constructed using SE-DEA approach, CCR input orientation, as shown below:

Inputs: PDD, AAE_obs, RAE, AEN_nsm

Outputs: AEE_pred, TNS.

RESULTS AND DISCUSSION

The dataset consists of 223 public vocational schools whose courses were divided into 12 technological axes plus high school (CPS, 2018). Two typologies of use were identified and agricultural schools were excluded from the dataset and only conventional vocational schools were selected given the significant difference in the profile of use.

Initial features of the model: The features used in the predictive model were chosen in order to test the hypothesis of their statistical significance in the energy consumption of each teaching unit. Furthermore, four new features related to the climate and three features related to the effective were created. Cooling degrees-day (CDD), as discussed in Meng and Mourshed (2017) and Golden *et al.* (2017), was used to assess the impact of climatic conditions on energy consumption and they were calculated using climatic data from a typical reference year (USFC, 2016) of the closest city to each school. Thus, two balance point temperatures (Bt) were tested in the CDD construction: dry bulb temperature of 20 °C (CDD_DB20), and wet bulb temperature of 17 °C (CDD_WB17). Since the CDD feature impacts more significantly buildings with large air-conditioned areas, a weighting was made taking into account the proportion of the area under CDD. Considering CBA as the air-conditioned area and BUA is the constructed area for each school, the feature ACBt = (CBA / BUA) × CDD_Bt was created, with Bt being the balance point temperature for the two tested cases. The total number of students (TNS) stands for to the sum of students in different periods, and the adjusted number of students (NSA) also refers to the same sum, but it considers a double weight to the number of full time students and it was created in order to test the hypothesis of the larger weight of them. The feature SCC = ESD + MAB + CPD + SEC + HSC

means the sum of the number of students in technological axes with similarity to the infrastructure, and it was created as a form of dimensionality reduction. Data of energy consumption referring to the period from January to December of 2017 were collected in energy bills and data of use and population of the buildings were collected from the staff of the schools. Thus, after the removal of agricultural schools and outliers, the final dataset for the predictive model has a total of 91 vocational schools. As the model was constructed aiming to predict monthly energy consumption, it has the total of 1,092 observations for training and testing. The raw data and description of each feature is in a public repository available in (SILVA, 2018).

Features selection of predictive model: The Pearson correlation coefficient (r) test for each feature in relation to consumption (ENE) was performed, and the features with r values less than 0.20 were excluded from the model. In addition, an analysis of the correlation between continuous predictor features was also done in order to exclude the ones with multicollinearity problems. The selection was finalized with the choice of the feature MTH (categorical feature equivalent to the reference month) as a way of capturing the seasonality in energy consumption. The climatic features did not present significant correlation and were excluded from the model.

The final model represented by X_n (predictor features), and Y_n (objective features) was:

X_n : TNS, BUA, CIP, EIXAGR, IPD, IFS, EHA, IAC, SCD, MTH; and
 Y_n : ENE

Development and test of the predictive model: For the elaboration, development and testing of the predictive model the Python programming language version 3.6.5 was used, and the dataset was divided in the proportion of 70% of the data for the training set, which is equivalent to 764 records, and 30% of the data for the test set, which corresponds to 328 records. The training of the predictive model was performed using MVS algorithm where the RBF kernel function was selected, and the values of $C = 3.9E3$, $\epsilon = 0.1$, $\gamma = 0.09$ were used in the finalized model. The application of the metrics to the test set, when the predicted values were compared to the actual values, obtained the R^2 of 0.90, the RMSE of 2,252.87 kilowatt-hour and a CV-RMSE of 18.30%.

Energy benchmarking between vocational schools: The method was applied in all schools, excluding agricultural schools and schools where no data were available for the selected period. Thus, the method was applied in 72 vocational schools. The calculation of the performance features was done by using the model previously trained with the whole dataset for predicting the monthly energy consumption of the 72 vocational schools, as well as the calculation of the respective annualised values. The other features were also calculated for all vocational schools and the final model with the complete set of features is available in (SILVA, 2019). The DEA analysis was performed using the SE-DEA and it was implemented in Python programming language. In order to compare each DMU with the others on a scale of efficiency, an analysis of the accumulated frequency of the efficiencies was created with five levels, from A to E, where A is the most

efficient. A normality test, which was applied upon the calculated efficiencies, rejected the normality hypothesis and the log-logistic distribution was used, since the Kolmogorov-Smirnov test, considering a significance level of 5%, resulted in a p-value of 0.4334, which means no evidence to reject the null hypothesis. Thus, the five levels of the scale were divided according to percentiles shown in Figure 2.

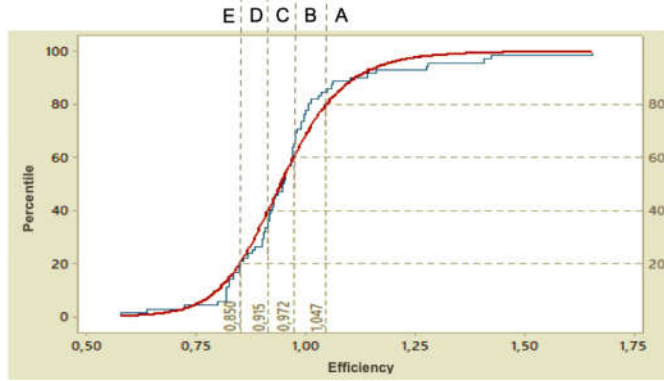


Figure 2. Accumulated efficiency frequency

Thus, discriminating each DMU by its calculated efficiency for each category, and then considering schools classified as A and B as efficient, schools level C as typical and D and E as inefficient, the final result is shown in Figure 3.

Grade	DMU	Grade	DMU	Grade	DMU	Grade	DMU	Grade	DMU	Grade	DMU
A	12	B	45	C	10	D	51	E	255	E	207
	227		226		40		14		199		254
	17		208		97		218		13		98
	66		59		64		11		205		282
	108		154		26		117		103		61
	8		34		23		200		128		268
	19		244		142		6		221		7
	36		225		115		230		141		140
224	78	41	229	85	76						
170	91	256		9	151						
16	247	118		123	253						
67	220	228		186	240						
145	43	88									

Figure 3. Efficiency scale for all DMUs

Conclusion

The proposed benchmarking scale allows a global assessment of the level of efficiency regarding to energetic metrics, permitting the formulation of policies backed by decision support tools. Nevertheless, the proposed method can be implemented for energy management in any use typology of buildings, since customized features for the portfolio are selected in order to characterize the performance. The main merit of the method lies in the fact that the insertion of the other features extrapolates the analysis beyond the energy consumption and encompasses managerial issues. From the 72 schools included in the benchmarking mechanism, 26 schools were considered efficient (grades A and B), 22 were considered typical schools (grades C), and 24 were considered inefficient schools (grades D and E). Considering only the inefficient schools, the annual potential of energy saving, taking into account the waste of energy and comparing it to the predicted energy consumption and the actual consumption, is 259,846 kilowatt hour, which represents an average value of 10,827 kilowatt-hour per school. High values of reactive energy were also observed and it summed 396,219 kilovolt-ampere-reactive resulting in an annual value of 44,336 kilovolt-ampere-reactive above efficient schools. Furthermore, the cumulative deviation

in the contracting demand was 1,197 kilowatt, and this amount was billed monthly. It is also important to highlight that the average consumption ratio between the non-school months and the school months is 0.66 for all the efficient schools, while this value is 0.76 for inefficient schools, which indicates high energy consumption in non-school months when compared to more efficient schools. These numbers show a great potential for saving energy and financial resources, especially in the buildings classified as inefficient by the method when compared to the best practices.

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